

66. Since we will be taking the vector cross product in the course of our calculations, below, we note first that when the two vectors in a cross product $\vec{A} \times \vec{B}$ are in the xy plane, we have $\vec{A} = A_x \hat{i} + A_y \hat{j}$ and $\vec{B} = B_x \hat{i} + B_y \hat{j}$, and Eq. 3-30 leads to

$$\vec{A} \times \vec{B} = (A_x B_y - A_y B_x) \hat{k} .$$

Now, we choose coordinates centered on point O , with $+x$ rightwards and $+y$ upwards. In unit-vector notation, the initial position of the particle, then, is $\vec{r}_0 = s \hat{i}$ and its later position (halfway to the ground) is $\vec{r} = s \hat{i} - \frac{1}{2} h \hat{j}$. Using either the free-fall equations of Ch. 2 or the energy techniques of Ch. 8, we find the speed at its later position to be $v = \sqrt{2g|\Delta y|} = \sqrt{gh}$. Its momentum there is $\vec{p} = -M\sqrt{gh} \hat{j}$. We find the angular momentum using Eq. 12-18 and our observation, above, about the cross product of two vectors in the xy plane.

$$\vec{\ell} = \vec{r} \times \vec{p} = -sM\sqrt{gh} \hat{k}$$

Therefore, its magnitude is $|\vec{\ell}| = sM\sqrt{gh}$.