

# Teoria da Computação

## MIEI 2018/2019 - FCT UNL

### Aula Prática 3

#### Modelling with Sets and Logic

1. Consider a system that keeps track of the access permissions regarding a set of printers within a network. Consider that for each user there is a set printers that (s)he is allowed to use.
  - (a) Model the set of states of the system with a set *APRINTER*.
  - (b) Model (with a function or relation) the operation that checks if a user has access to a specific printer.
  - (c) Model (with a function or relation) the operation that gives a user access to a printer.
  - (d) Model (with a function or relation) an operation that returns the users that can access more printers.
2. Consider a system that keeps track of playlists. A playlist includes a name and a set of songs. Each song is defined by a title, an artist or band name, a duration, and a rating (1 to 5).
  - (a) Model the set of states of the system with a set *SPLAYLIST*.
  - (b) Model (with a function or relation) the operation that adds a song to a playlist.
  - (c) Model (with a function or relation) the operation that removes a song from a playlist.
  - (d) Model (with a function or relation) the operation that removes a song from all playlists.
  - (e) Model (with a function or relation) the operation that given a song name returns the playlist names that include the song.
3. Model the following system with a structure.

Consider a simplified version of *Google<sup>+</sup> Circles* where a user organizes friends using circles. A circle is simply a collection of users identified by a name. A user can be added to more than one circle. Assume that each user is identified by an email.

  - (a) Model *SCIRCLE*, the set of states of the system.
  - (b) Define (with a function or relation) the operation on *SCIRCLE* that adds a user to a set of circles.
  - (c) Define (with a function or relation) the operation on *SCIRCLE* that retrieves all people in a circle.
  - (d) Define (with a function or relation) the operation on *SCIRCLE* that blocks a user, i.e., deletes a user from all circles.
  - (e) Define (with a function or relation) the operation on *SCIRCLE* that retrieves all the circles associated with a given user.

- (f) Define (with a function or relation) the operation on *SCIRCLE* that given a user, retrieves its larger circle.
- (g) Define (with a function or relation) the operation on *SCIRCLE* that given two circles names, retrieves the users that belong to the intersection.
- (h) An extended circle of an user are its circle's circles, i.e. people who are at one degree of distance.  
Define (with a function or relation) the operation on *SCIRCLE* that given a user, retrieves its extended circle.