

# DERIVADAS

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Sejam  $u \equiv u(x)$  e  $v \equiv v(x)$  funções reais de variáveis reais.

1.  $c' = 0, \quad c = \text{constante}$

2.  $x' = 1$

3.  $(u \pm v)' = u' \pm v'$

4.  $(cu)' = cu', \quad c = \text{constante}$

5.  $(uv)' = u'v + uv'$

6.  $\left(\frac{u}{v}\right)' = \frac{u'v - uv'}{v^2}$

7.  $(u^r)' = r u^{r-1} u', \quad r \in \mathbb{R}$

8.  $(\sqrt[n]{u})' = \frac{u'}{n \sqrt[n]{u^{n-1}}}, \quad n \in \mathbb{N}$

9.  $(e^u)' = u' e^u$

10.  $(a^u)' = a^u u' \ln a, \quad a \in \mathbb{R}^+$

11.  $(\ln(u))' = \frac{u'}{u}$

12.  $(\log_a(u))' = \frac{1}{\ln a} \frac{u'}{u}$

13.  $(u^v)' = u^v v' \ln(u) + v u^{v-1} u'$

14.  $(\sin(u))' = u' \cos(u)$

15.  $(\cos(u))' = -u' \sin(u)$

16.  $(\tan(u))' = \frac{u'}{\cos^2(u)} = u' \sec^2(u)$

17.  $(\cot(u))' = -\frac{u'}{\sin^2(u)} = -u' \operatorname{cosec}^2(u)$

18.  $(\sec(u))' = u' \sec(u) \tan(u)$

19.  $(\operatorname{cosec}(u))' = -u' \operatorname{cosec}(u) \cot(u)$

20.  $(\arcsen(u))' = \frac{u'}{\sqrt{1-u^2}}$

21.  $(\arccos(u))' = -\frac{u'}{\sqrt{1-u^2}}$

22.  $(\arctan(u))' = \frac{u'}{1+u^2}$

23.  $(\arccot(u))' = -\frac{u'}{1+u^2}$

24.  $(\operatorname{arcsec}(u))' = \frac{u'}{u\sqrt{1+u^2}}$

25.  $(\operatorname{arccosec}(u))' = -\frac{u'}{u\sqrt{1-u^2}}$

26.  $(\operatorname{senh}(u))' = u' \cosh(u)$

27.  $(\cosh(u))' = u' \operatorname{senh}(u)$

28.  $(\operatorname{tgh}(u))' = \frac{u'}{\cosh^2(u)} = u' \operatorname{sech}^2(u)$

29.  $(\operatorname{cotgh}(u))' = -\frac{u'}{\operatorname{senh}^2(u)} = -u' \operatorname{cosech}^2(u)$

30.  $(\operatorname{sech}(u))' = -u' \operatorname{tgh}(u) \operatorname{sech}(u)$

31.  $(\operatorname{cosech}(u))' = -u' \operatorname{cotgh}(u) \operatorname{cosech}(u)$

32.  $(\operatorname{argsh}(u))' = \frac{u'}{\sqrt{u^2+1}}$

33.  $(\operatorname{argch}(u))' = \frac{u'}{\sqrt{u^2-1}}$

34.  $(\operatorname{argtgh}(u))' = \frac{u'}{1-u^2}$

35.  $(\operatorname{argcotgh}(u))' = \frac{u'}{1-u^2}$

36.  $(\operatorname{argsech}(u))' = -\frac{u'}{u\sqrt{1-u^2}}$

37.  $(\operatorname{argcosech}(u))' = -\frac{u'}{u\sqrt{1+u^2}}$