

$$\begin{vmatrix} \frac{\partial^2 f}{\partial x^2} & \frac{\partial^2 f}{\partial x \partial y} \\ \frac{\partial^2 f}{\partial y \partial x} & \frac{\partial^2 f}{\partial y^2} \end{vmatrix}$$

$$4u^2y$$

$$\frac{\partial^2 f}{\partial x^2} = (2(x^2+y^2) \cdot 2x - 4x)' = (4x^3 + 2y^2 \cdot 2x - 4x)' = 12x^2 + 4y^2 - 4$$

$$\frac{\partial^2 f}{\partial y^2} = (2(x^2+y^2) \cdot 2y - 4y)' = (4y^3 + 2x^2 \cdot 2y - 4y)' = 4y^2 + 12x^2 - 4$$

$$D = A \times B - C^2$$

$$\begin{vmatrix} 12x^2 + 4y^2 - 4 & 4y^2 + 12x^2 - 4 \\ 4y^2 + 12x^2 - 4 & 4y^2 + 12x^2 - 4 \end{vmatrix}$$

$$= (12 + 2 - 4)(4 + 12 - 4) =$$

$$= (12 - 2)(4 + 12 - 4) =$$

$$= (10)(12) = 120$$

$$(120) > 0$$

$$\frac{\partial^2 f}{\partial x^2} > 0 \Rightarrow \text{minimum}$$

$$u^2 = 24$$

$$\begin{vmatrix} 12u^2 + 4y^2 - 4 & 8yn \\ 8yu & 4u^2 + 12y^2 - 4 \end{vmatrix}$$

$$\frac{\partial^2 f}{\partial u \partial y} = \frac{\partial}{\partial y} \left(\frac{\partial f}{\partial u} \right) =$$

$$K u^{\frac{1}{2}} = K u'$$

$$\frac{\partial}{\partial y} (4u^3 + 4y^2u - 4u) = 4u \cdot 2y = 8yu$$

$$\frac{\partial}{\partial x} (4x^2 + 12y^2 - 4) = (8x)$$

$$8yu =$$

$$12 \times 12 - 8 \times 8 = 144 - 64 = 80$$